

## 1.7. Long Multiplication and Division Review

Multiplication of large numbers is done using the distributive property of multiplication over addition. The numbers are first split into ones, tens, hundreds, etc.

$$259 \cdot 5 = (200 + 50 + 9) \cdot 5 = 200 \cdot 5 + 50 \cdot 5 + 9 \cdot 5$$

An **algorithm** known as **long multiplication** is used to simplify writing:

|         |                              |                |
|---------|------------------------------|----------------|
| 5       |                              |                |
| × 2 5 9 |                              |                |
| 4 5     | multiply the <b>ones</b>     | 5 · 9 ones     |
| 2 5     | multiply the <b>tens</b>     | 5 · 5 tens     |
| + 1 0   | multiply the <b>hundreds</b> | 5 · 2 hundreds |
| 1 2 9 5 |                              |                |

**Example 1:** Multiply integers: 67 and 8.

|       |       |
|-------|-------|
| 6 7   | 8     |
| × 8   | × 6 7 |
| 5 3 6 | 5 6   |
|       | 4 8   |
|       | 5 3 6 |

**Practice 1:** Calculate:

$$\begin{array}{r} 65 \\ \times 3 \\ \hline \end{array}$$

$$\begin{array}{r} 24 \\ \times 4 \\ \hline \end{array}$$

$$\begin{array}{r} 19 \\ \times 5 \\ \hline \end{array}$$

$$\begin{array}{r} 36 \\ \times 5 \\ \hline \end{array}$$

$$\begin{array}{r} 18 \\ \times 7 \\ \hline \end{array}$$

$$\begin{array}{r} 23 \\ \times 6 \\ \hline \end{array}$$

$$\begin{array}{r} 2 \\ \times 56 \\ \hline \end{array}$$

$$\begin{array}{r} 4 \\ \times 12 \\ \hline \end{array}$$

$$\begin{array}{r} 3 \\ \times 99 \\ \hline \end{array}$$

$$\begin{array}{r} 3 \\ \times 45 \\ \hline \end{array}$$

$$\begin{array}{r} 3 \\ \times 61 \\ \hline \end{array}$$

$$\begin{array}{r} 4 \\ \times 82 \\ \hline \end{array}$$

**Example 2:** Multiply 619 and 7 using long multiplication.

$$\begin{array}{r} 619 \\ \times \quad 7 \\ \hline 4313 \end{array}$$

multiply the ones  $619 \cdot 7$  ones

Start by multiplying ones  $9 \cdot 7 = 63$ . Write ones (3) at ones spot, and carry the 6.

Multiply tens and add the 6 that was carried over  $1 \cdot 7 + 6 = 7 + 6 = 13$ . Write tens (3) at the tens spot and carry the 1.

Multiply hundreds and add the 1 that was carried over  $6 \cdot 7 + 1 = 42 + 1 = 43$ . Write hundreds (3) at the hundreds spot and carry the 4.

There are no thousands in this problem, so just use the 4 that was carried over to the thousand column.

**Practice 2:** Calculate:

$$\begin{array}{r} 215 \\ \times \quad 2 \\ \hline \end{array}$$

$$\begin{array}{r} 216 \\ \times \quad 2 \\ \hline \end{array}$$

$$\begin{array}{r} 370 \\ \times \quad 3 \\ \hline \end{array}$$

$$\begin{array}{r} 308 \\ \times \quad 3 \\ \hline \end{array}$$

$$\begin{array}{r} 450 \\ \times \quad 5 \\ \hline \end{array}$$

$$\begin{array}{r} 601 \\ \times \quad 9 \\ \hline \end{array}$$

$$\begin{array}{r} 430 \\ \times \quad 8 \\ \hline \end{array}$$

$$\begin{array}{r} 304 \\ \times \quad 5 \\ \hline \end{array}$$

$$\begin{array}{r} 504 \\ \times \quad 3 \\ \hline \end{array}$$

$$\begin{array}{r} 901 \\ \times \quad 9 \\ \hline \end{array}$$

**Example 3:** Multiply 342 and 37 using long multiplication.

$$\begin{array}{r} \phantom{+} 342 \\ \times \phantom{+} 37 \\ \hline \phantom{+} 2394 \\ + 1026 \\ \hline 12654 \end{array}$$

multiply with **ones**  $342 \cdot 7$  ones  
multiply with **tens**  $342 \cdot 3$  tens

Start by multiplying the first factor, 342, by the ones digit of the second factor, 7, and write the result underneath the line:

$$342 \cdot 7 = (2 + 40 + 300) \cdot 7 = 14 + 280 + 2100 = 2394$$

Multiply 342 by the number of tens of the second factor, 3. Write the result aligned with the tens column.

$$342 \cdot 3 = (2 + 40 + 300) \cdot 3 = 6 + 120 + 900 = 1026$$

Finally add the two rows in order to get the final result of **12654**.

**Practice 3:** Multiply.

$$\begin{array}{r} 164 \\ \times 12 \\ \hline \end{array}$$

$$\begin{array}{r} 235 \\ \times 15 \\ \hline \end{array}$$

$$\begin{array}{r} 705 \\ \times 35 \\ \hline \end{array}$$

$$\begin{array}{r} 214 \\ \times 13 \\ \hline \end{array}$$

$$\begin{array}{r} 221 \\ \times 64 \\ \hline \end{array}$$

$$\begin{array}{r} 453 \\ \times 23 \\ \hline \end{array}$$

**Example 4:** Divide  $124 \div 4$  using long division.

$$\begin{array}{r} 31 \\ 4 \overline{)124} \\ \underline{12} \phantom{0} \\ 04 \\ \underline{4} \\ 0 \end{array}$$

**Example 5:** Divide  $175 \div 7$  using long division.

$$\begin{array}{r} 25 \\ 7 \overline{)175} \\ \underline{14} \phantom{0} \\ 35 \\ \underline{35} \\ 0 \end{array}$$

**Practice 4:** Divide the following integers. Use long division.

a)  $328 \div 8 =$

b)  $295 \div 5 =$

c)  $426 \div 6 =$

d)  $576 \div 8 =$